

# Coupling a Regional Climate Model to a Lake Tile Model for Prediction of Dissolved Oxygen Profiles in Lakes

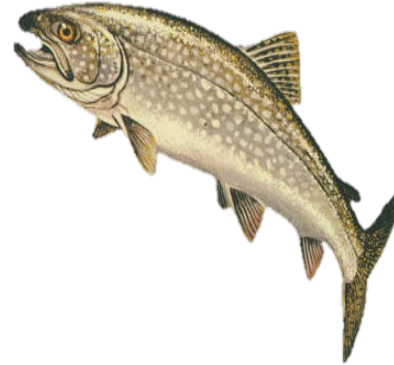
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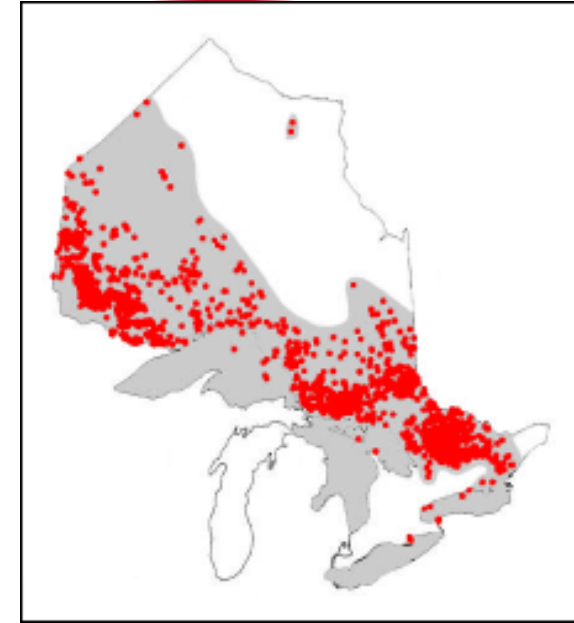
## Outline

- Part I: Introduction
- Part II: Bottom boundary layer mixing sub-models
- Part III: Photosynthesis and water column respiration
- Part IV: Summary and Conclusions

## Lake Trout



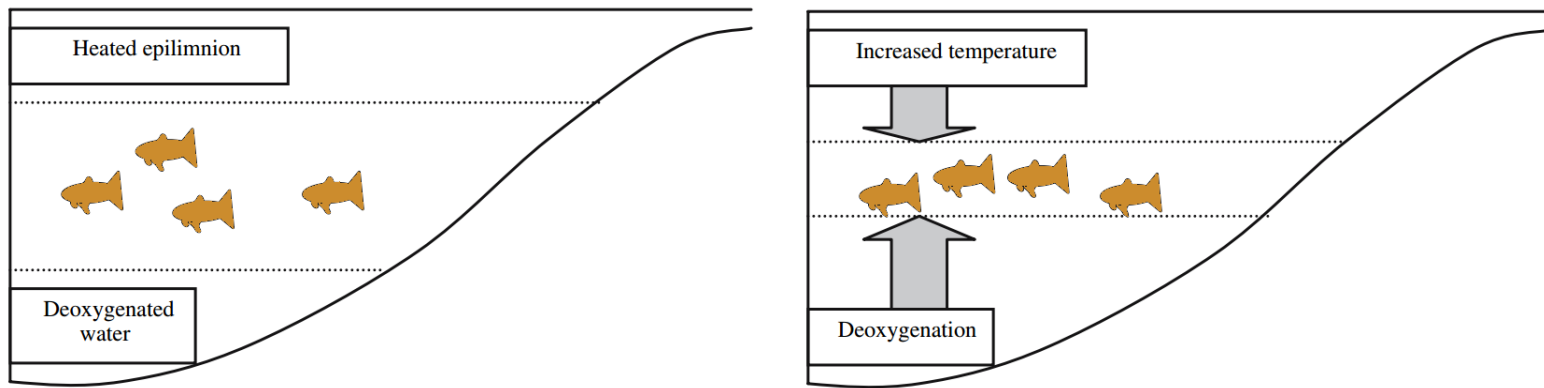
- length: 30-80 cm, weight: 1-5 kg  
Ontario record: 28.6 kg
- Valuable ecologically and economically
- Great importance to Ontario's recreational fisheries:  
over \$2.5 billion to the provincial economy  
(OMNR 2014)



*Lake Ontario, Lake Huron,  
Lake Superior and across  
the deep, cold lakes of the  
Canadian Shield  
([www.ontario.ca](http://www.ontario.ca))*

# Introduction

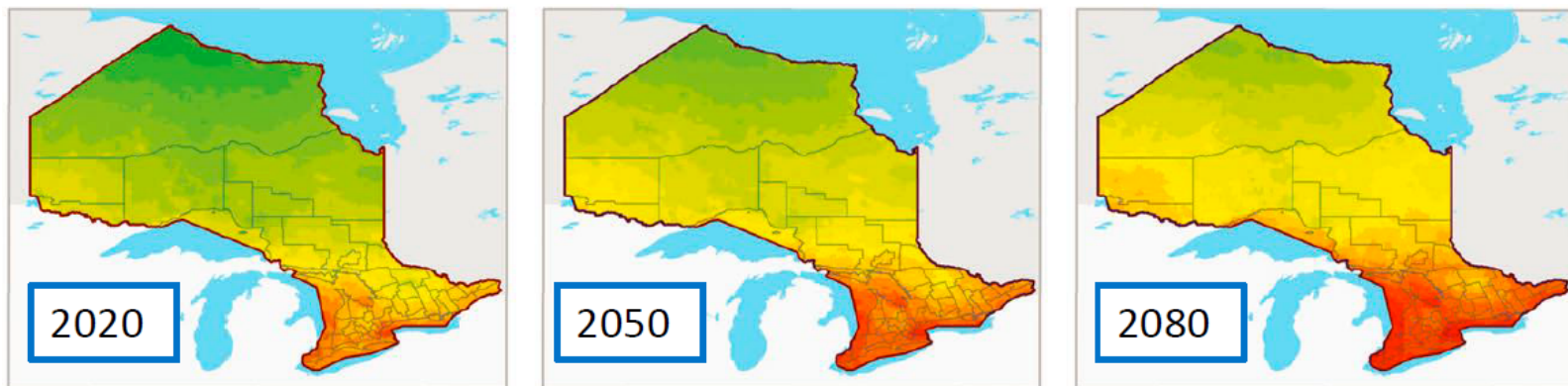
- Narrow tolerances for temperature (T) and dissolved oxygen (DO)  
Temperature: 6-15°C  
DO: 9-12 mg/L
- Vulnerable to many stresses including climate warming:  
Increased T  $\implies$  Thicker Epilimnion  
Increased fish metabolism  $\implies$  Decreased concentrations of DO



*Effect of climate change on restriction of habitat availability for Lake Trout (Ficke et al., 2007)*

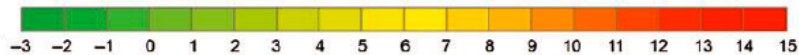
# Introduction

- Significant weather changes in central Canada by 2100 (GCM):  
Winter: increase by 3-5°C  
Summer: increase by 3-4°C (low greenhouse gas emission scenarios)  
Climate changes → lower water levels → less hypolimnion volumes  
→ severe hypoxia

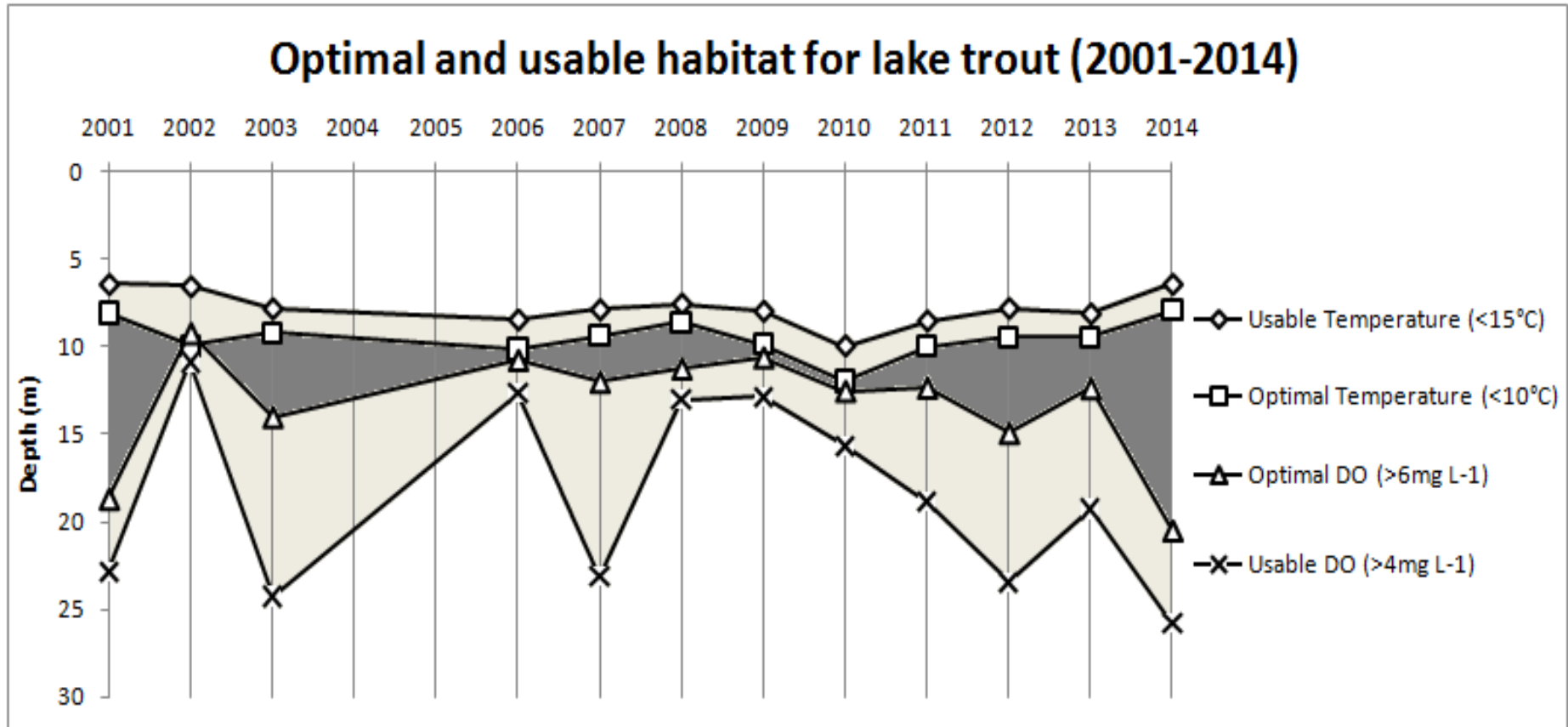


Annual mean temperature (C)

(Wang et al., 2014)

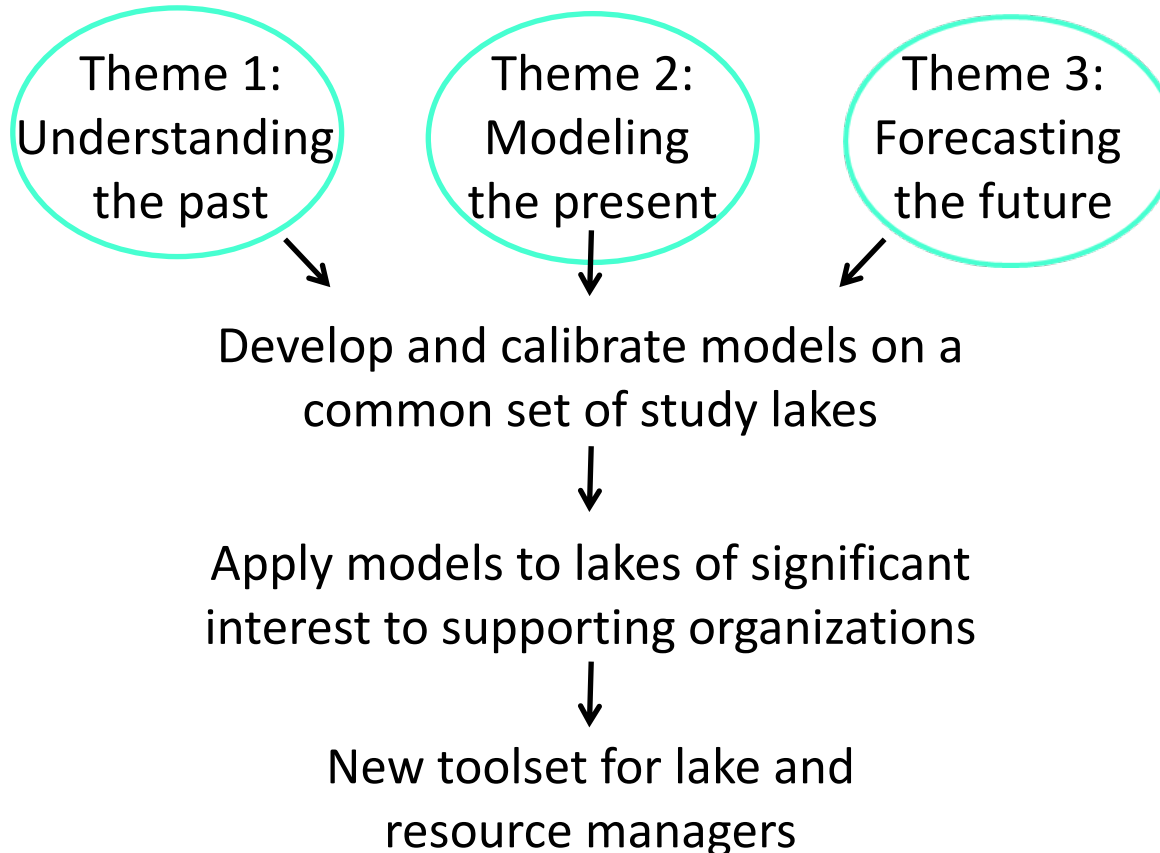


# Lake Trout habitat in Eagle Lake

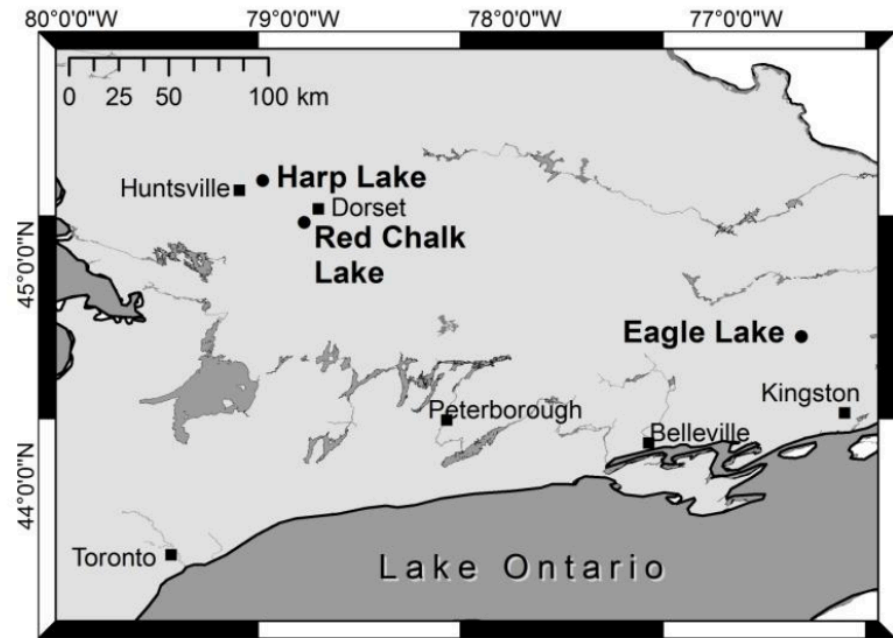


# Project Overview

- A 3-part study to:
  - Analyze sediment cores to understand the past
  - Develop empirical formulae to model the present
  - Apply computational models to forecast the future



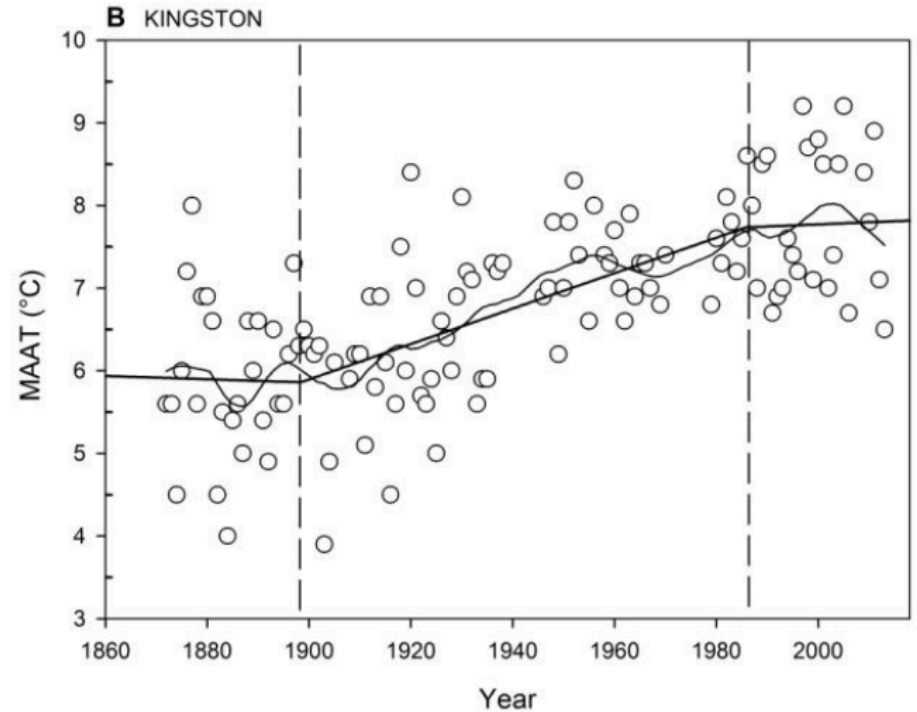
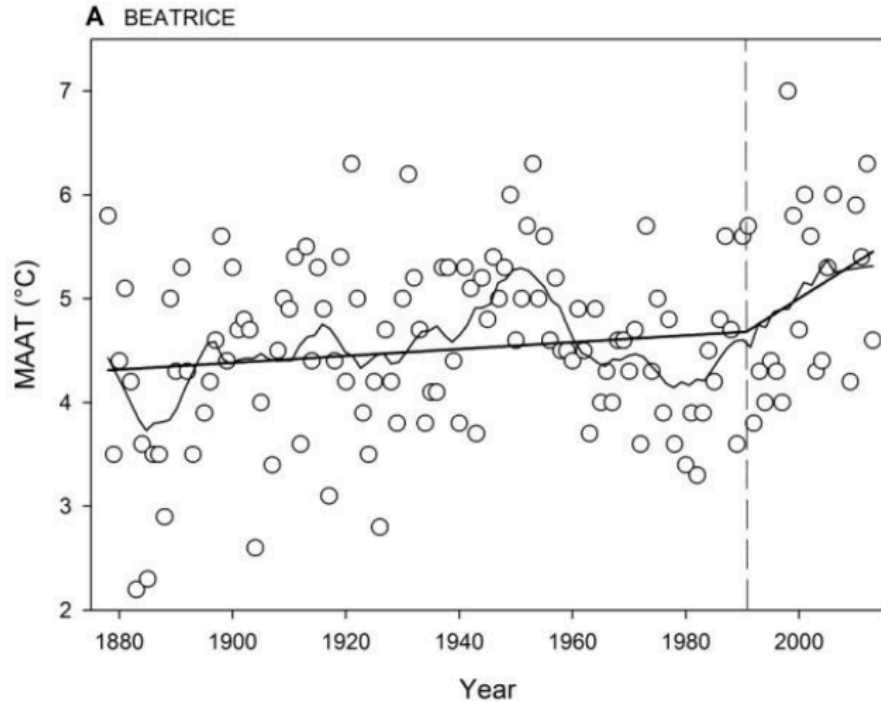
# Harp Lake and Eagle Lake



Variable	Harp Lake	Eagle Lake
$Z_{\max}$ (m)	37.5	31.1
TP ( $\mu\text{g/L}$ )	5.74	9.00
DOC (mg/L)	4.41	4.05
pH	6.42	7.9
Surface Area ( $\text{km}^2$ )	0.71	6.65
Length of shoreline (km)	4.74	41.4
Number of cottages	~100	>300



# Historical warming near Harp and Eagle Lakes



*A) Mean annual air temperature (MAAT) from a climate station located in Beatrice ~35 km from Harp (B) MAAT from Kingston located ~50 km south of Eagle Lake.*

# Methods

- 1D bulk mixed-layer thermodynamic Canadian Small Lake Model (CSLM) embedded in Canadian Regional Climate Model (CRCM)
- Lakes represented as 1 m<sup>2</sup> watercolumn tiles (Mosaic approach)
- Hundreds of small lakes represented with a few idealized lake tiles
- Surface mixed layer model for surface layer with no mixing below SML (MacKay 2012)

- Added a simple DO sub-model (Hamilton and Schladow 1997)

- DO flux at surface and SOD applied to the first cell

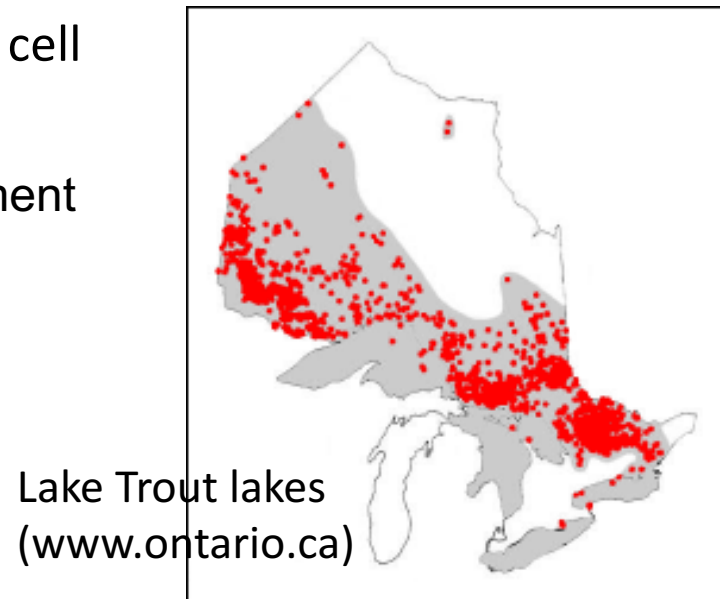
$$SOD = \mu_b DO / (DO + K_m) \alpha_{sed}^{T-20}$$

$\mu_b = 0.46 \text{ gm}^{-2}\text{d}^{-1}$  (maximum biochemical sediment oxygen uptake)

$K_m = 1.5 \text{ mgL}^{-1}$  (half saturation constant )

$\alpha_{sed} = 1.08$  (sediment temperature multiplier)

$T = \text{water temperature}$



# Harp Lake: model set-up

- **Calibration and validation:**

30 years of bi-weekly observations

July 5<sup>th</sup>, 1978 to December 31<sup>th</sup>, 2007

Maximum depth: 34 m

Square root of the surface area: 843 m

Extinction coefficient: 0.5 1/m

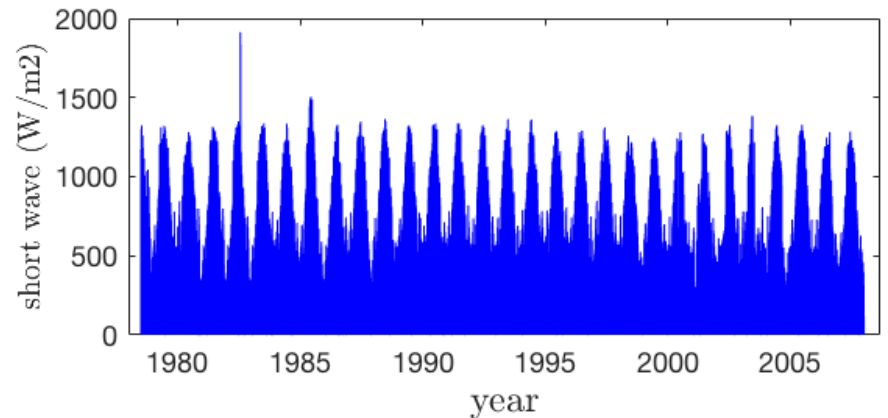
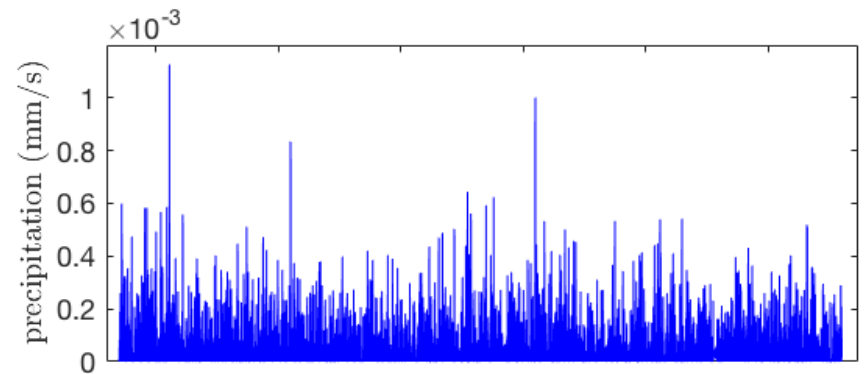
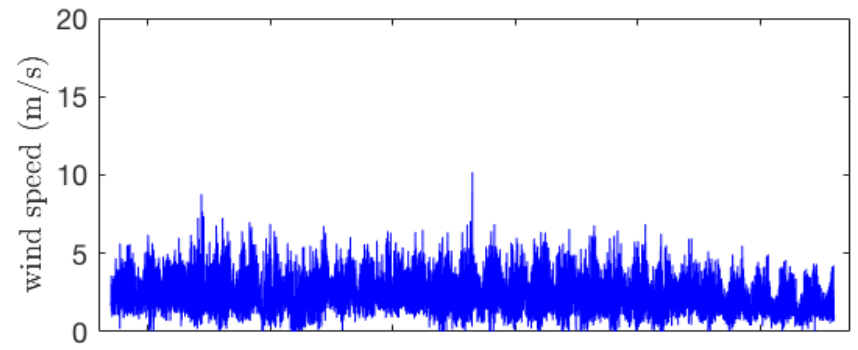
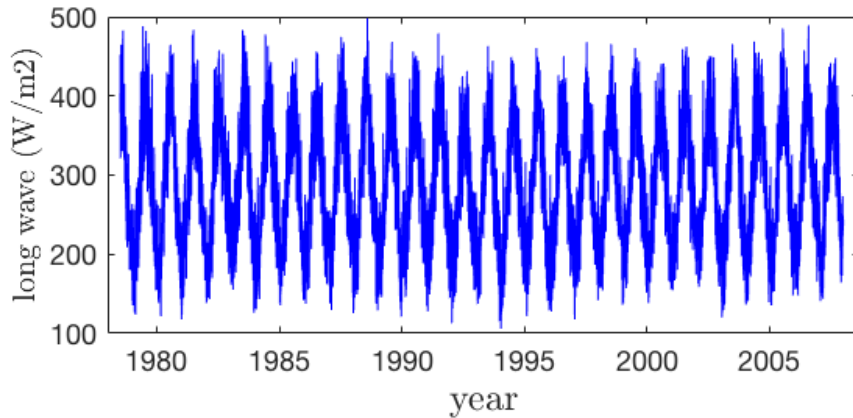
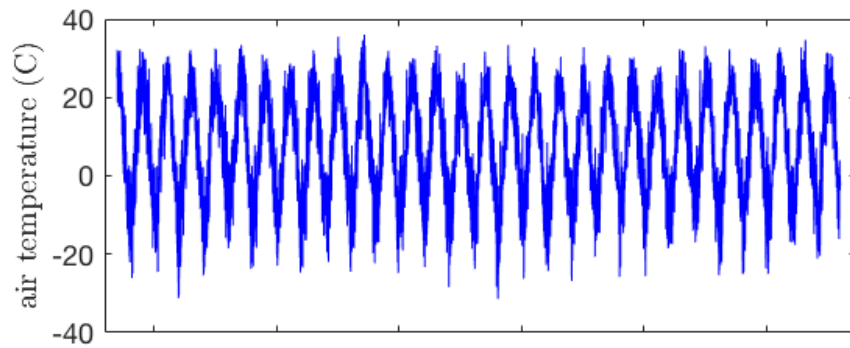
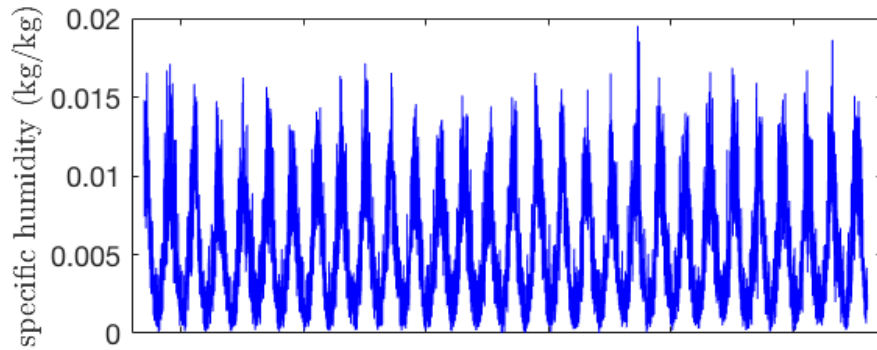
Grid spacing: 0.5 m

Time steps: 10 min

HOD= 0.03 gm<sup>-3</sup>d<sup>-1</sup>



# Harp Lake: Meteorology



# Eagle Lake: model set-up

- **Calibration and validation:**

5 years of high-frequency (10 s to 10 min) observations

June 22<sup>nd</sup>, 2011 to July 29<sup>th</sup>, 2015

Maximum depth: 30 m

Square root of the surface area: 250 m

Extinction coefficient: 0.3 1/m

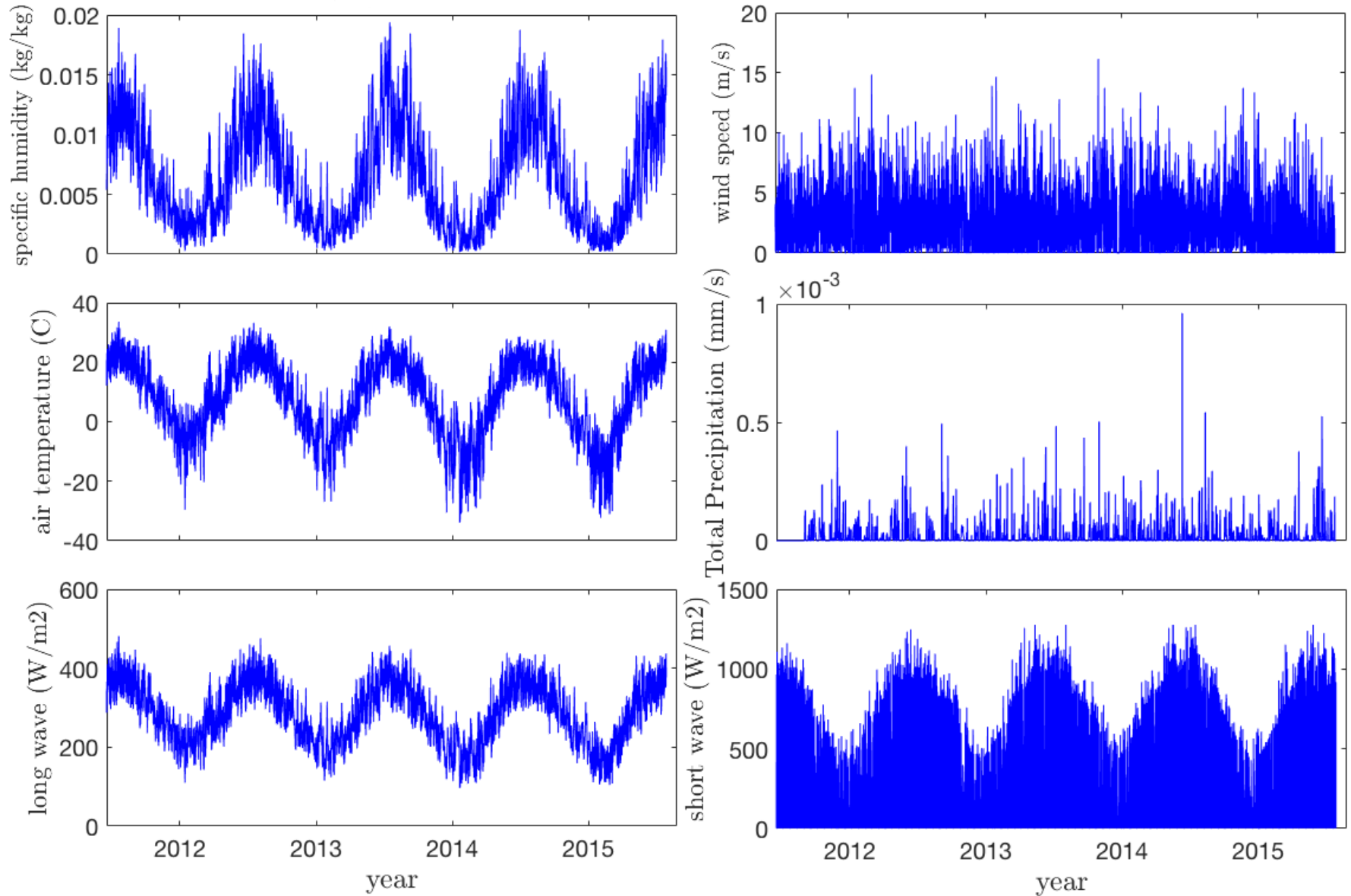
Grid spacing: 0.5 m

Time steps: 10 min

HOD= 0.08 gm<sup>-3</sup>d<sup>-1</sup>



# Eagle Lake: Meteorology



## Part II: Bottom boundary layer mixing sub-models

## Bottom boundary layer mixing sub-models

a)

- $h_{BML}$  following a mixed layer approach (Imberger, 1985; Spigel et al., 1986)
- Fully turbulent BML with uniform DO resulting from shear-induced mixing

$$d(uh_{BML})/dt = u_B^{*2}$$

$u$ : mixed-layer velocity

$u_B^*$ : bottom friction velocity ( $u_B^* = 0.2u_S^*$ )

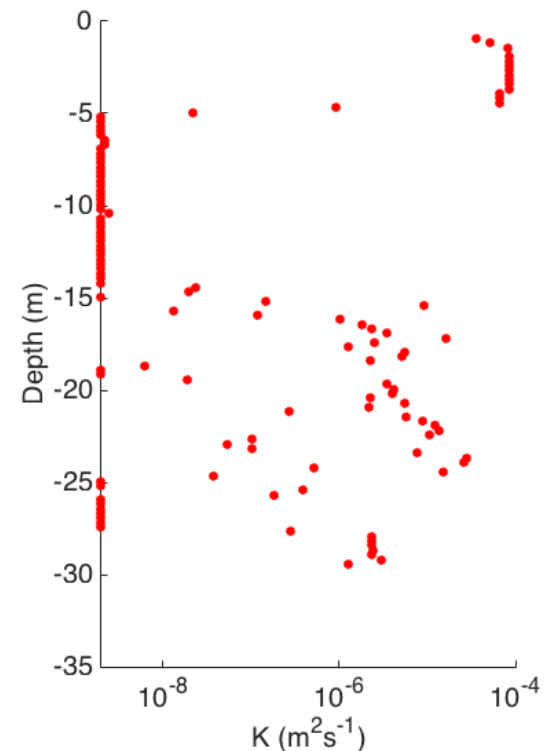
b)

- DO flux computed from Fick's Law

$$J = -K dDO / dz$$

$$K = 10^{-7} \text{ m}^2\text{s}^{-1}$$

$K$ : average diffusivity from microstructure profiler

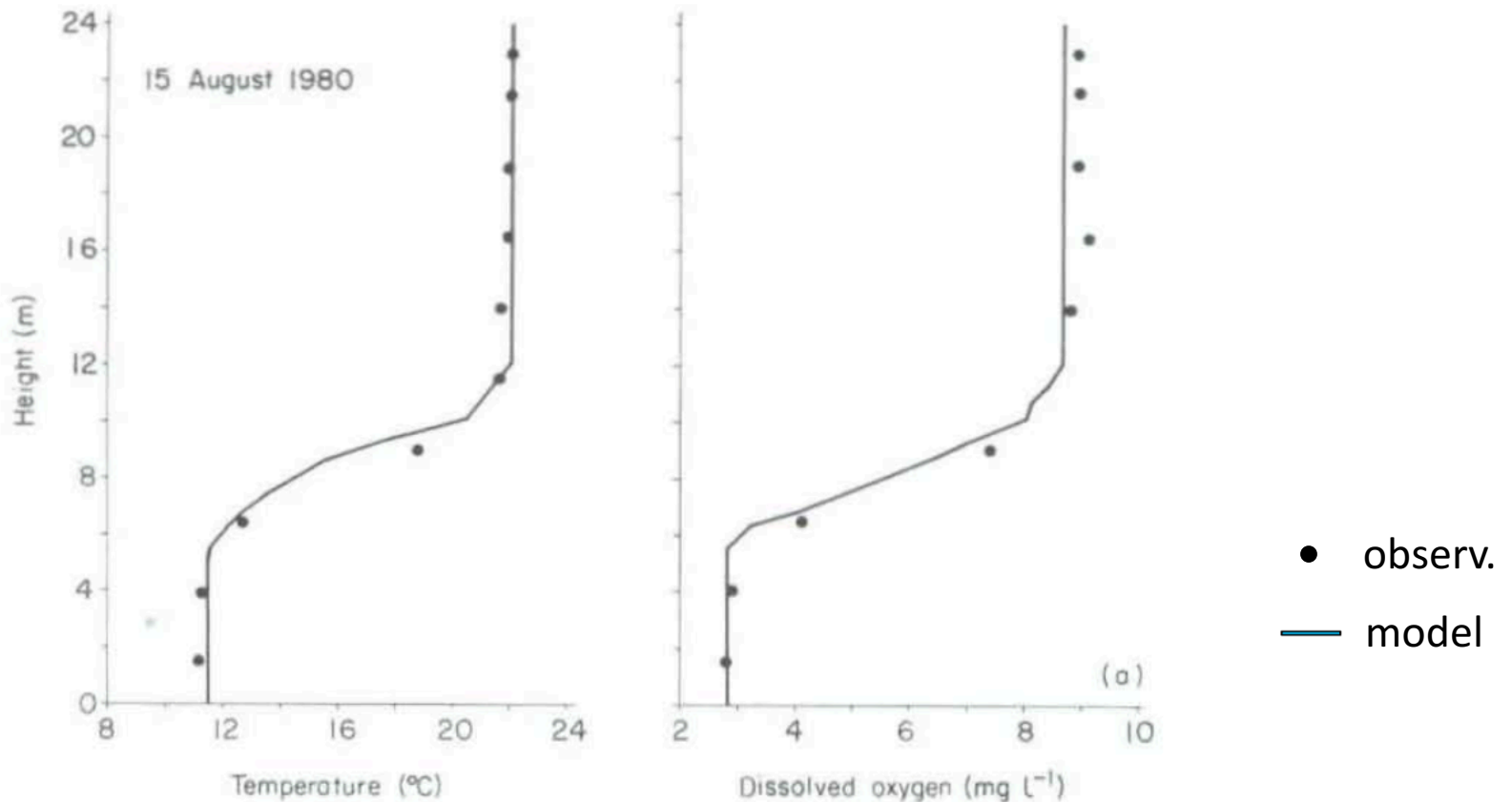




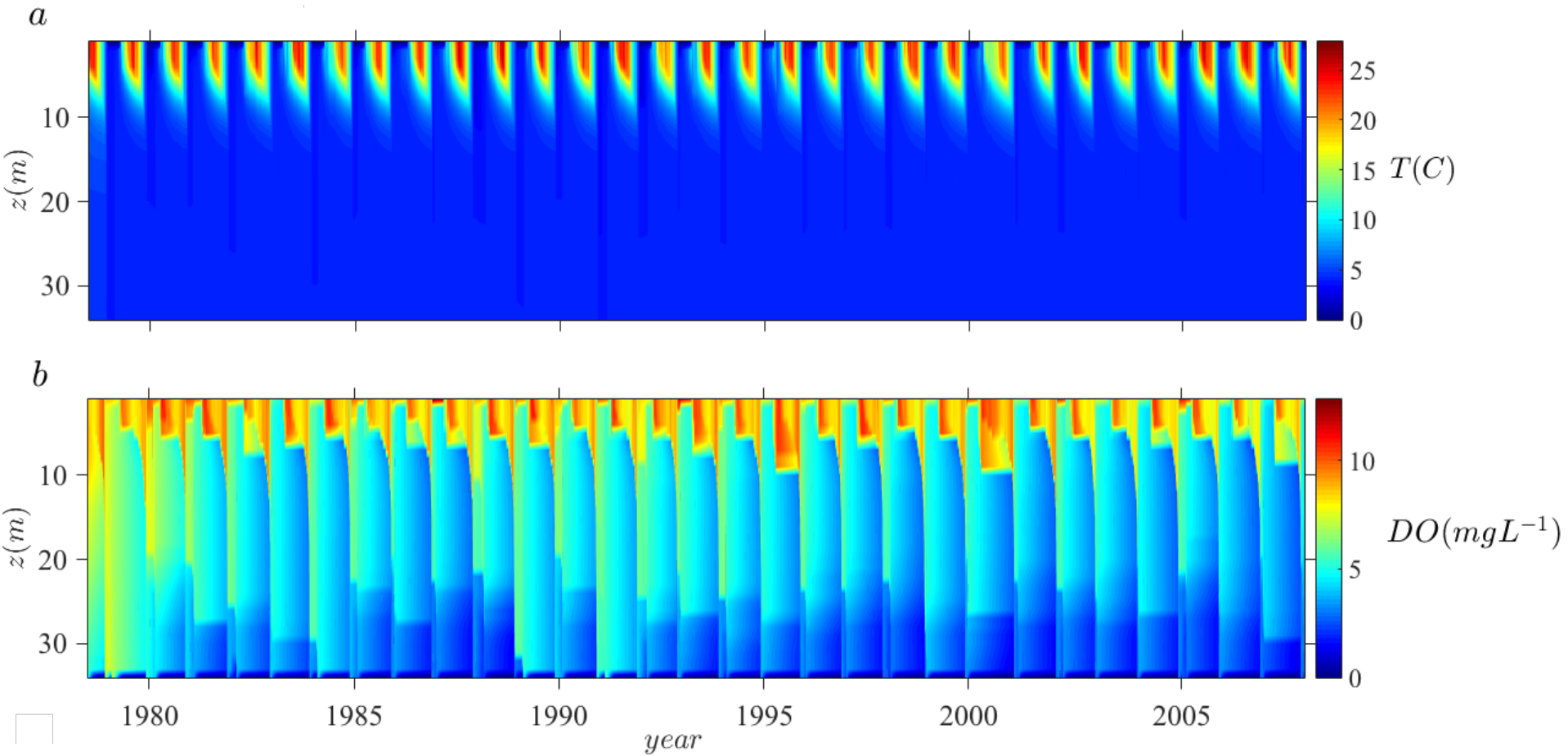
# Introduction

## Mixed-layer models in large lakes

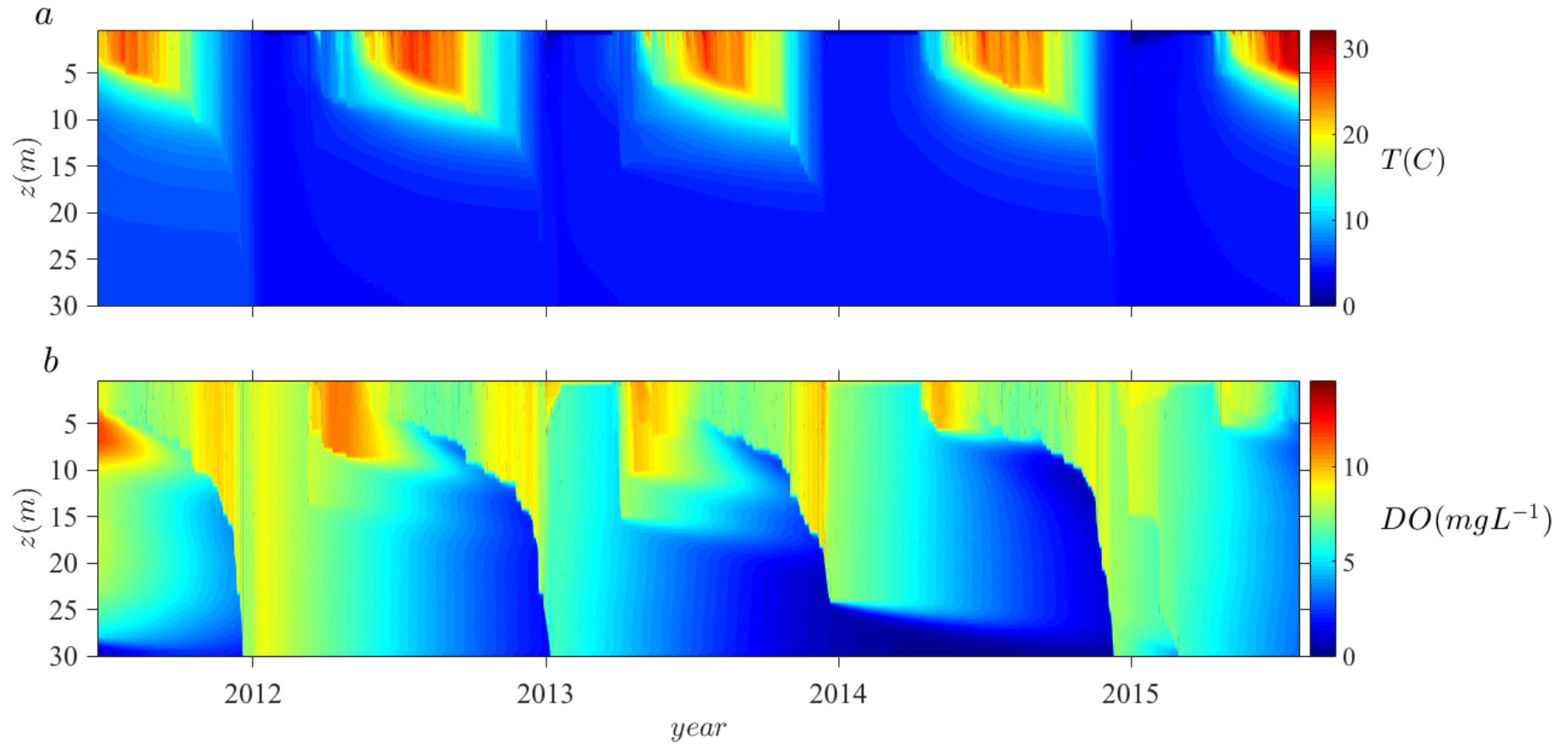
Lake Erie



# Harp Lake: Results

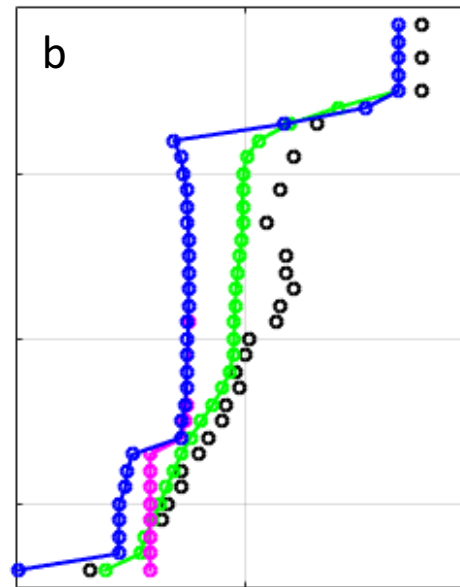
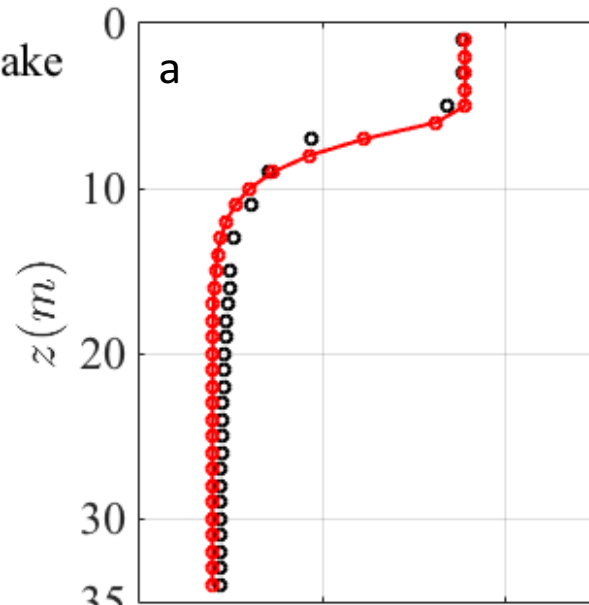


# Eagle Lake: Results



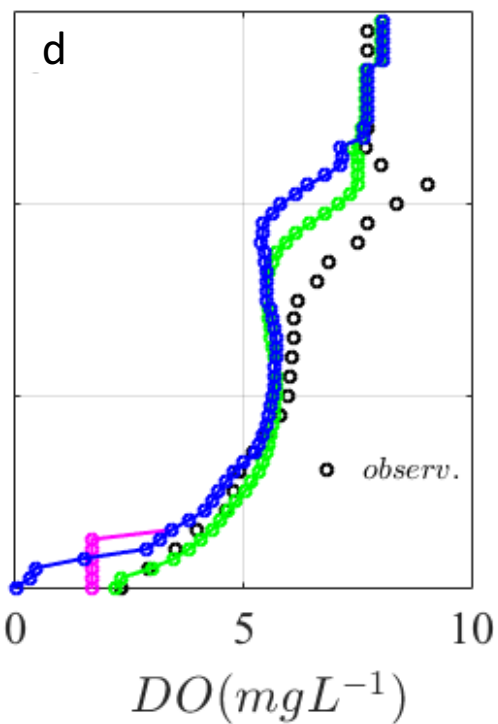
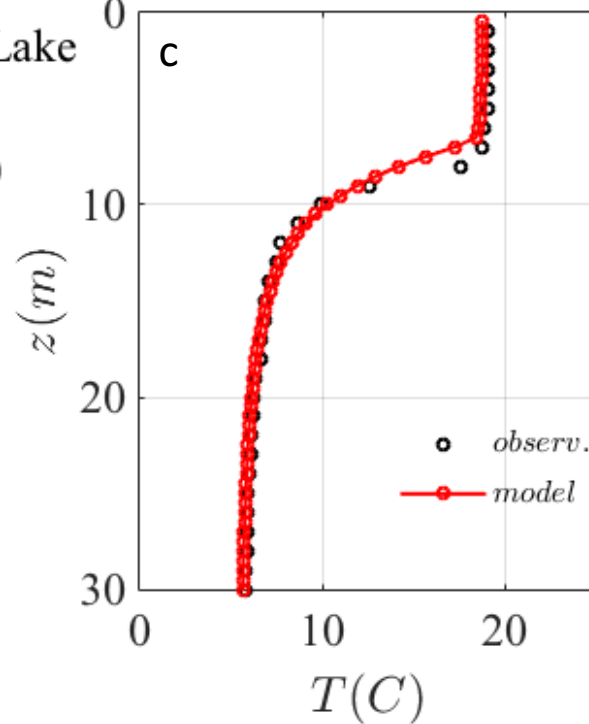
# Results

Harp Lake



a & b:  
Sep. 15<sup>th</sup>, 1999

Eagle Lake



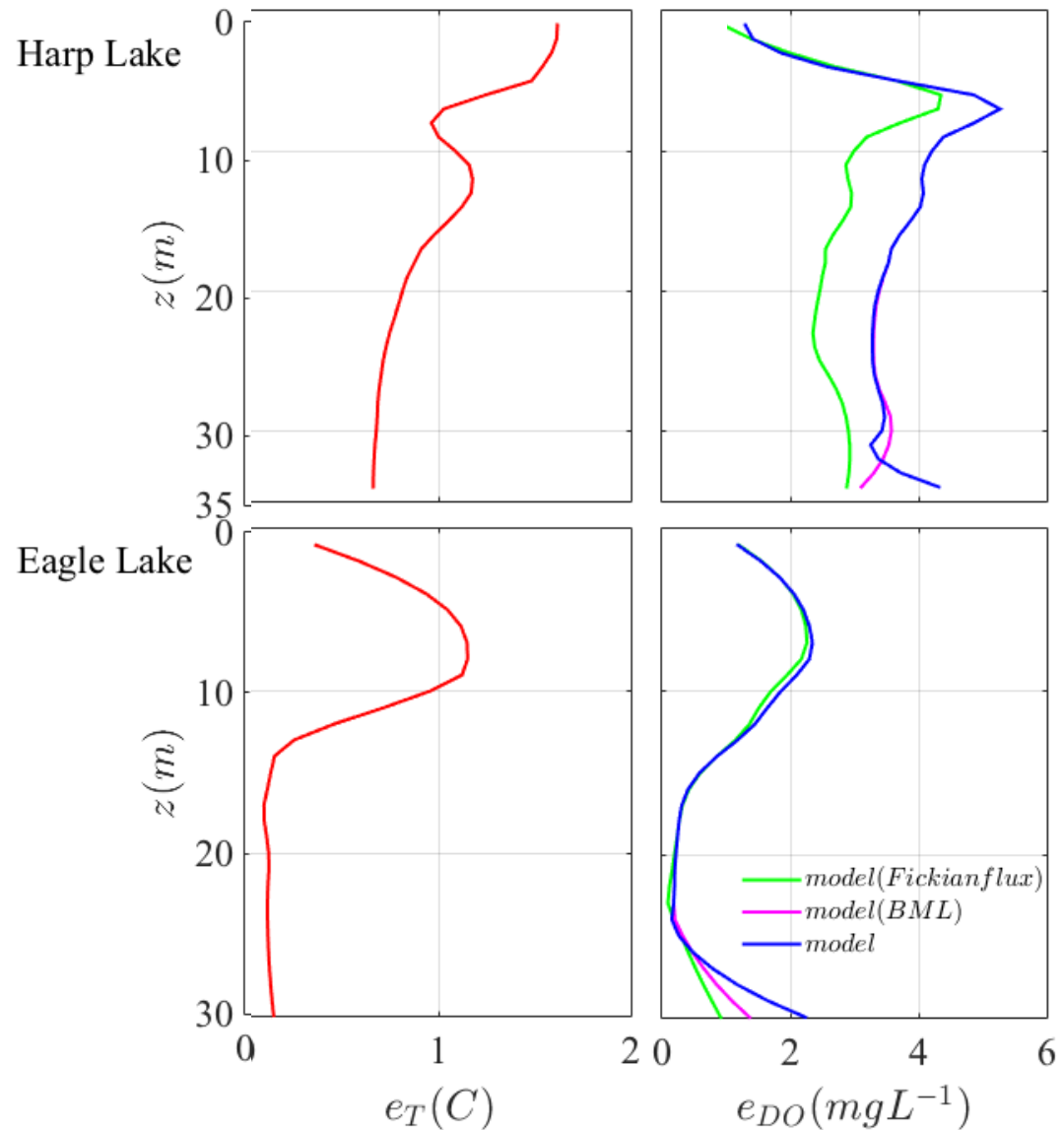
c & d:  
Sep. 22<sup>nd</sup>, 2011

— *model(Fickian flux)*  
— *model(BML)*  
— *model*

○ *observ.*  
—○ *model*

○ *observ.*

# Results RMSE



- Less error in DO prediction in BBL using the Fickian flux sub-model
- Smooth decrease in DO profiles using Fickian flux approach
- Fickian flux approach even improves DO predictions above the BBL
- Mixed layer approach is successful in the surface

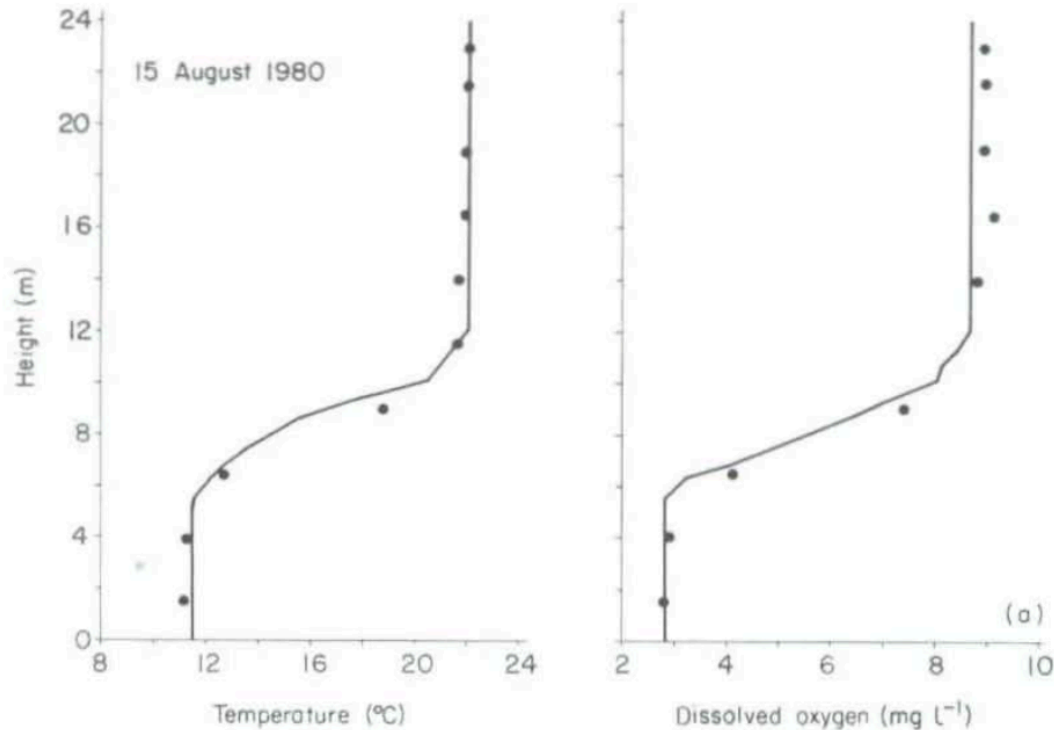
# Re dependence of mixed layer models

$$Re_{SML} = h_{SML} u^*_S / \nu$$

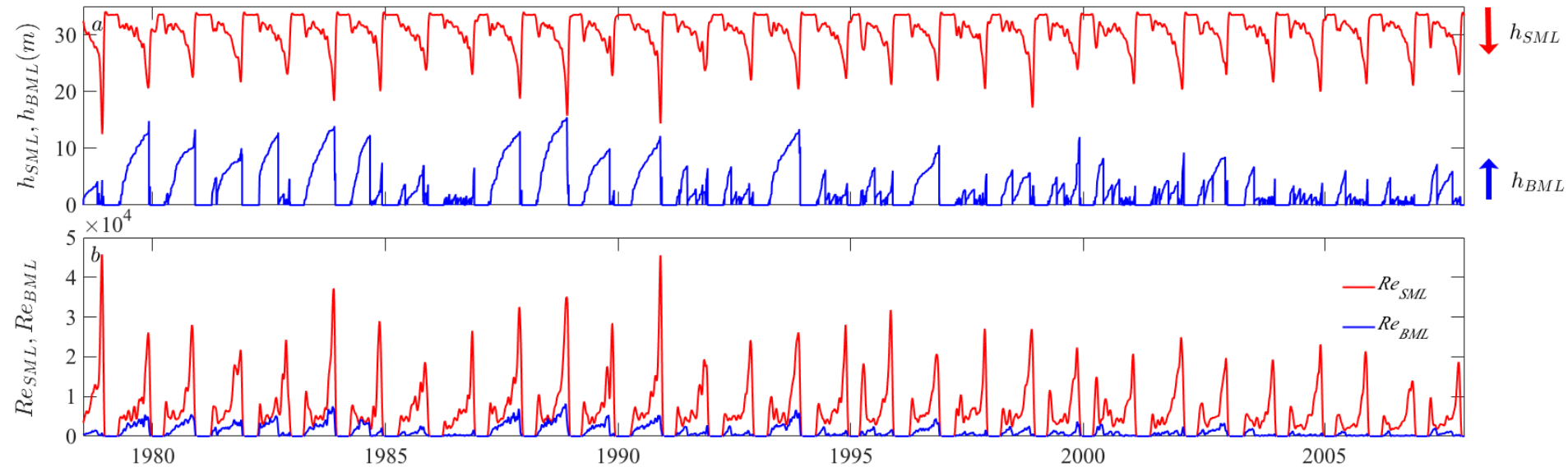
$$Re_{BML} = h_{BML} u^*_B / \nu$$

- In Lake Erie:  $u^*_B = 0.2$  cm/s and  $h_{BML} \approx 7$  m;  $Re_{BML} > 10,000$  and BML approach is successful

Lake Erie

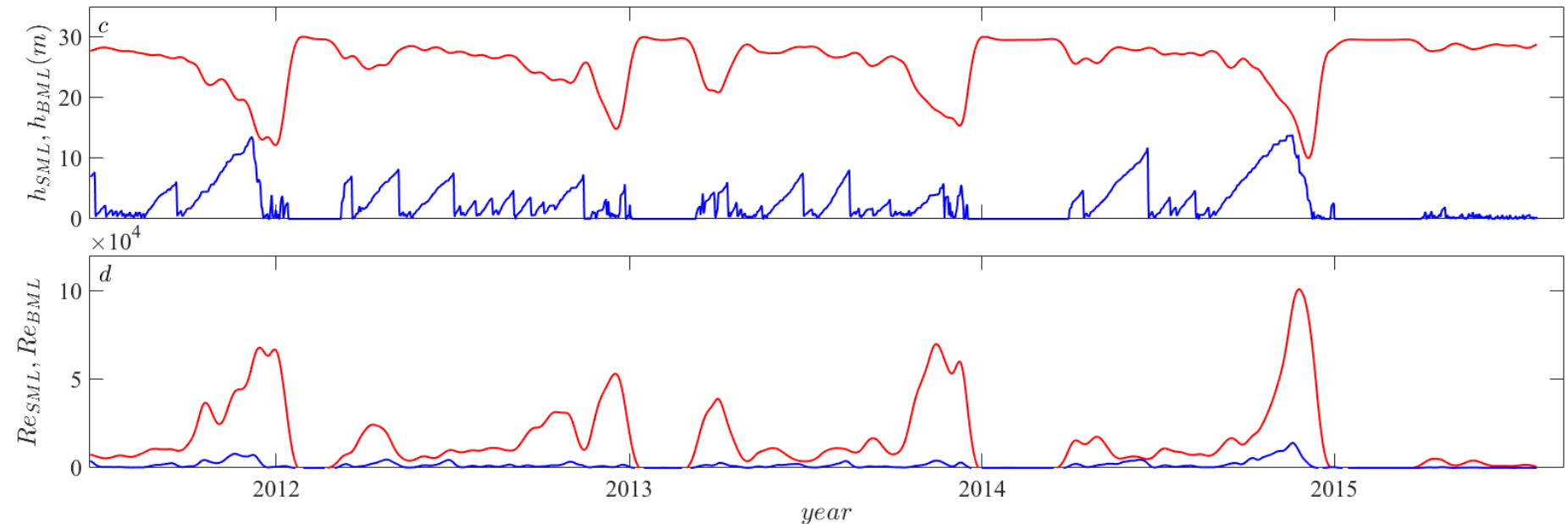


# Results: Harp Lake $Re$ and mixed layer height



- $h_{SML} > h_{BML}$ ;  $h_{BML} < 10$  m
- $Re_{BML} < Re_{SML}$ ;  $Re_{BML}$  barely exceeds 10,000  $\rightarrow$  BML approach is not accurate
- $Re_{SML} \geq 10,000$ ; higher turbulence at the surface  $\rightarrow$  SML approach is successful

# Results: Eagle Lake $Re$ and mixed layer height

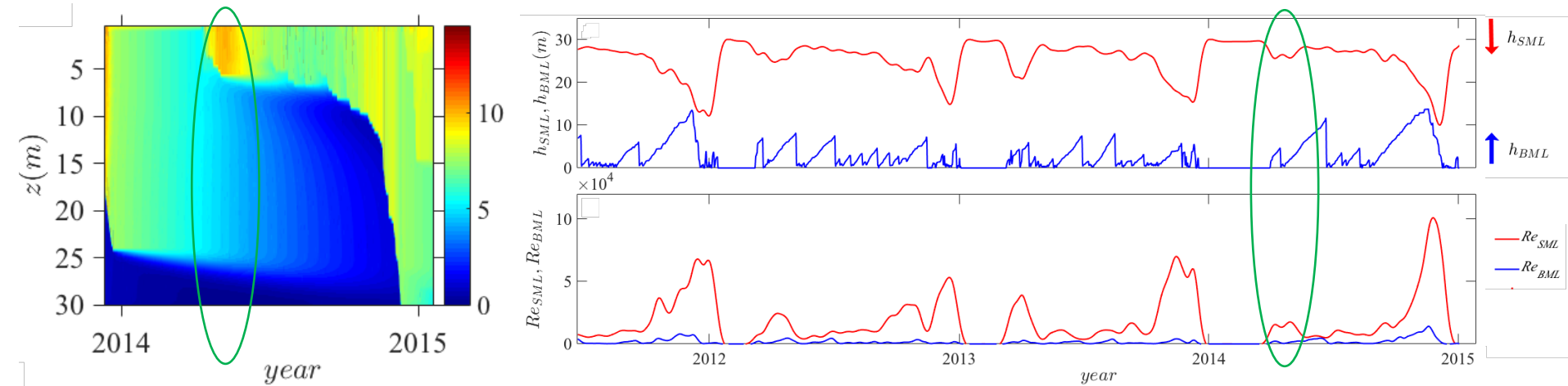


- $h_{SML} > h_{BML}$ ;  $h_{BML} < 10$  m
- $Re_{BML} < Re_{SML}$ ;  $Re_{BML}$  barely exceeds 10,000  $\rightarrow$  BML approach is not accurate
- $Re_{SML} \geq 10,000$ ; higher turbulence at the surface  $\rightarrow$  SML approach is successful



# Results: Mixing in turnover events

## Understanding deep-water hypoxia through $Re_{SML}$



- $Re_{SML}$  can be applied to understand lake turnover and re-oxygenation of the hypolimnion in spring and fall.
- Poor re-oxygenation of hypolimnion in spring 2014 turnover
- $Re_{SML} \approx 13,000$  ( $h_{SML} \approx 3\text{m}$ ) is low compared to  $Re_{SML}$  in other years



- Part III: Photosynthesis and water column respiration

# Methods

## Photosynthesis production

Parameterization of the specific production as a function of the light intensity  
(Platt et al., 1980)

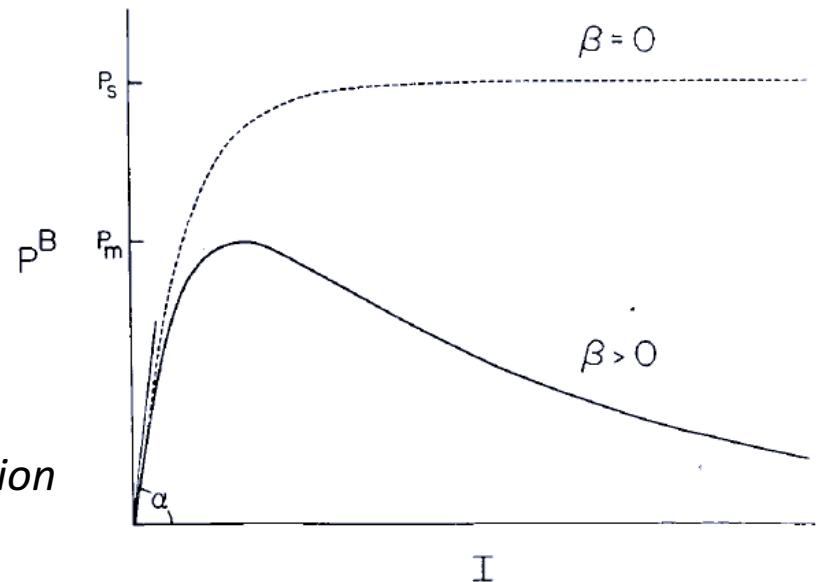
$$P^B = P_s^B \{1 - \exp(-\alpha I / P_s^B)\} \exp(-\beta I / P_s^B)$$

$P_s^B$ : Maximum potential specific productivity (41.5 mg O<sub>2</sub>/mg Chla/h)

$I$ : light intensity (W/m<sup>2</sup>)

$\alpha$ : 0.2 mg O<sub>2</sub> m<sup>2</sup> /mg Chla/hr/W

$\beta$ : 0.45 mg O<sub>2</sub> m<sup>2</sup> /mg Chla/hr/W



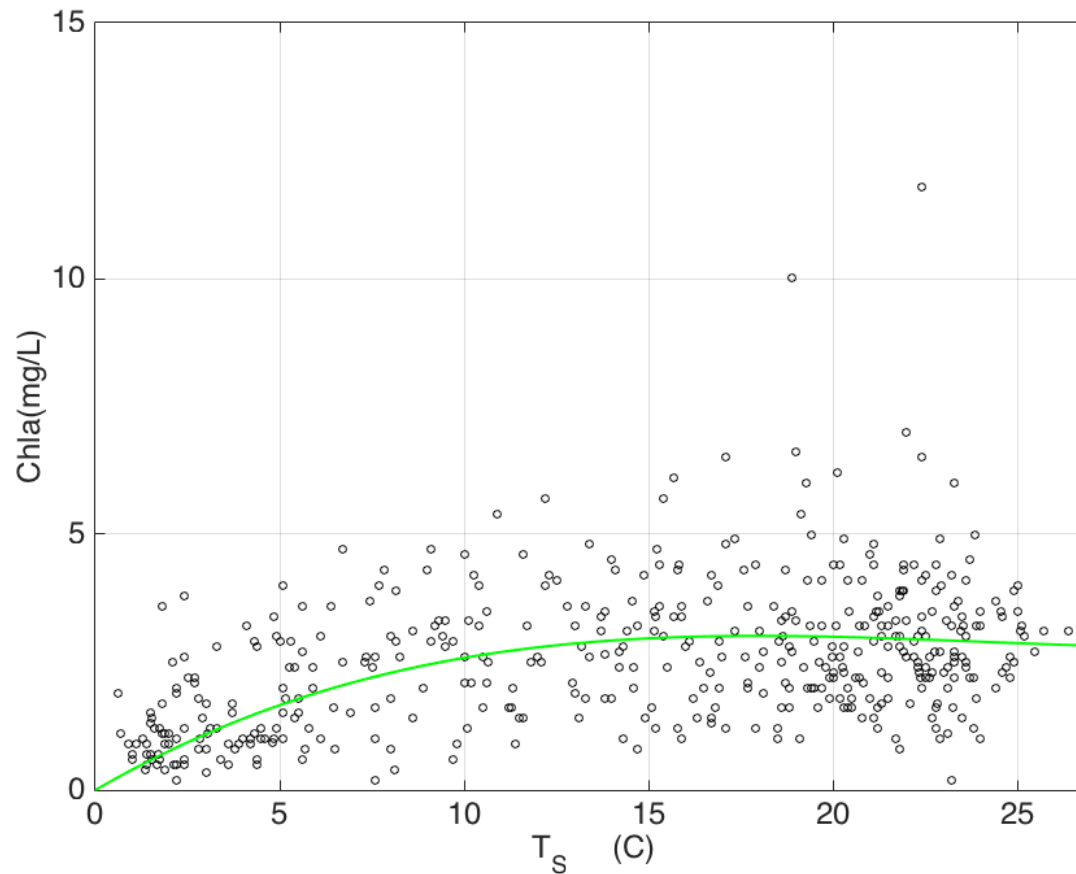
*General form of the function  
(Platt et al., 1980)*

# Methods

## Respiration

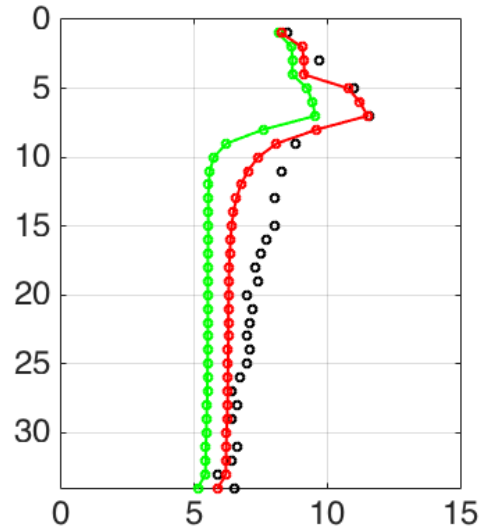
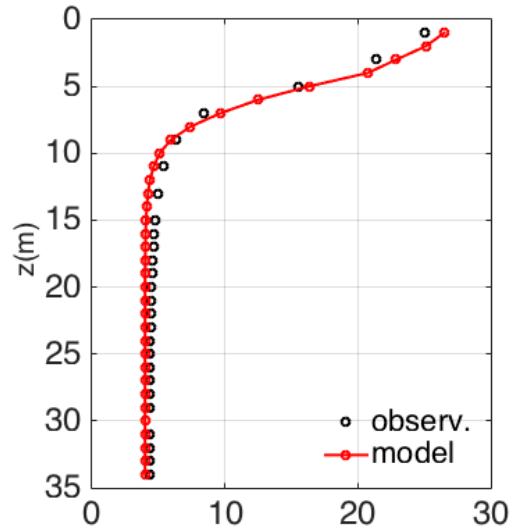
Respiration in upper mixed layer=1.8 photo-assimilation

Respiration in bottom mixed layer=0.2 photo-assimilation



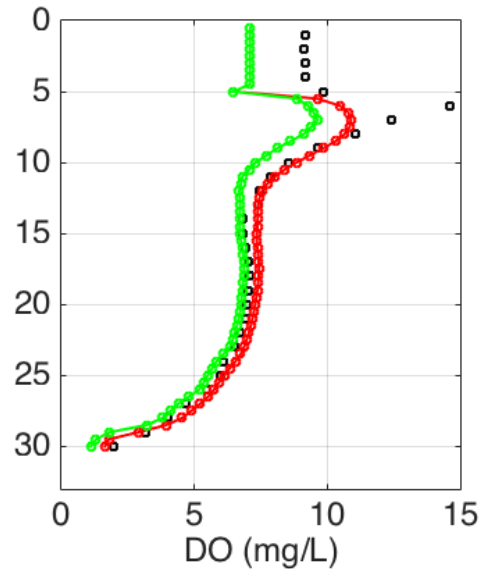
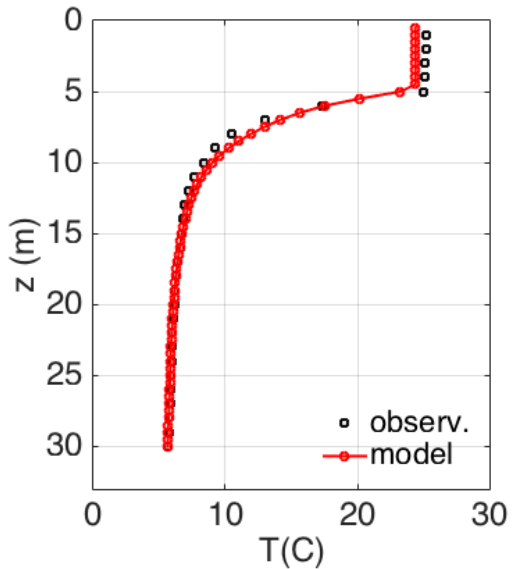
# Results

Harp Lake  
11 July 1988



○ observ.  
— Fickian (HOD 0.03 g/m<sup>3</sup>/d)  
— Fickian PRS

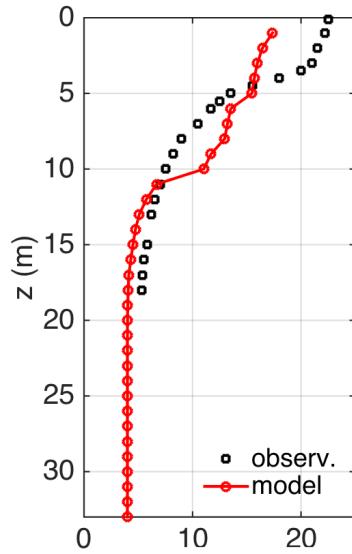
Eagle Lake  
8 August 2011



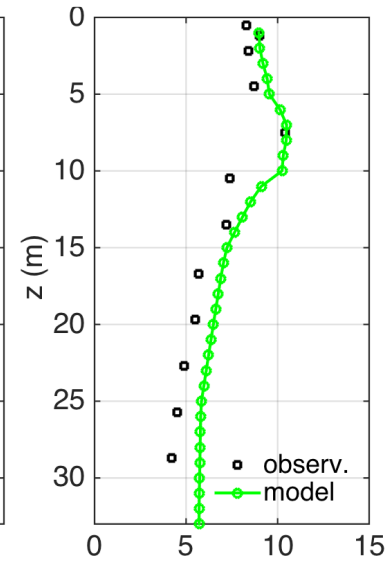
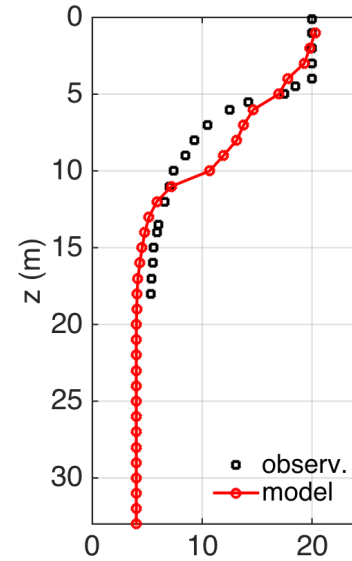
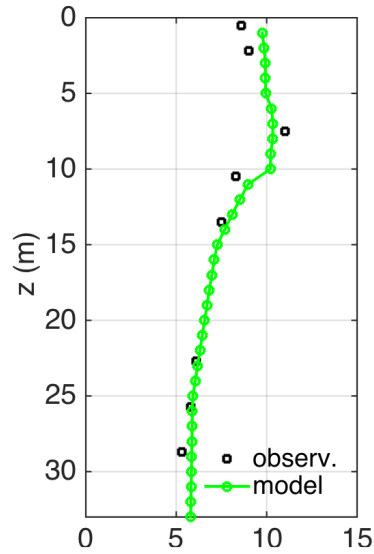
○ observ.  
— Fickian (HOD=0.08 g/m<sup>3</sup>/d)  
— Fickian PRS

# Results: Harp Lake GCM

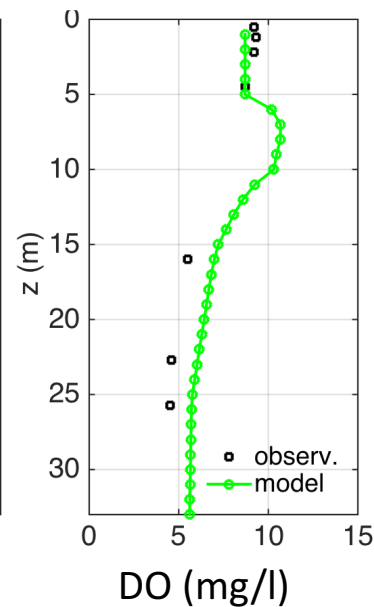
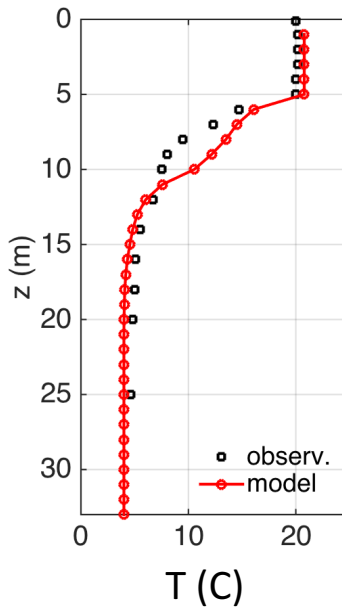
23 June  
1976



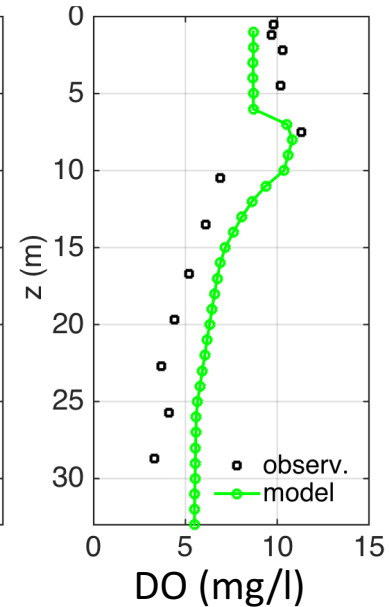
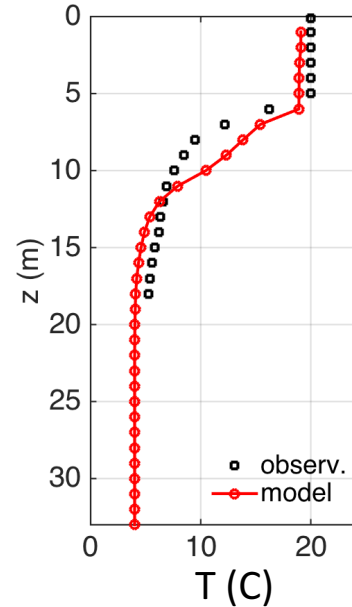
14 July  
1976



4 August  
1976



1 Septen  
1976



# Summary and Conclusions

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- In small lakes:  $Re_{BML} < Re_{SML}$ ;  $Re_{SML} > 10,000$  ( $Re_{BML}$  barely exceeds 10,000)
- For Reynolds numbers  $< 10,000$  the flow remains transitional and a Fickian diffusion model is appropriate
- For Reynolds numbers  $> 10,000$ , we expect a fully turbulent boundary layer and a mixed layer model should be used
- The best DO predictions are from the simple Fickian flux sub-model at the BBL, but a mixed layer approach in the surface
- Parameterization of the specific production as a function of the light intensity and respiration as a factor of photo-assimilation improves the results

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**Thank you!**